

PREDICTION OF FLOW PATTERNS AND FLOW BOILING HEAT TRANSFER OF CARBON DIOXIDE INSIDE HORIZONTAL TUBES

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Abstract. This talk describes the recent updated flow boiling heat transfer model and flow pattern map proposed by Cheng et al (2006) based on the flow boiling heat transfer mechanisms for horizontal tubes, methods that have been developed specifically for CO₂. First of all, the Wojtan et al. (2005a) flow pattern map was modified to fit the onset of dryout transition and the intermittent to annular flow transition observable in CO₂ heat transfer data. To adapt the Wojtan et al. (2005b) flow boiling model for low and medium pressure refrigerants to CO₂, several changes were found to be necessary. A new reduced pressure type of nucleate boiling heat transfer correlation was proposed for CO₂ based on the nucleate boiling contributions backed out of flow boiling heat transfer data at low vapor qualities and a nucleate boiling suppression was introduced into the model. The flow boiling heat transfer model predicted 75.5% of all the CO₂ database within $\pm 30\%$. The new model and map are applicable to: tube diameters (equivalent diameters for non-circular channels) from 0.8 to 10 mm, mass velocities from 170 to 570 kg/m²s, heat fluxes from 5 to 32 kW/m² and saturation temperatures from -28°C to 25°C (reduced pressures from 0.21 to 0.87). Several simulations of the updated map and heat transfer model are also shown here.

Keywords. Flow boiling, Heat transfer, Flow map, Flow patterns, CO₂

1. Introduction

Carbon dioxide has received significant interest in the past decade as an environmentally safe refrigerant for automotive air conditioning, low temperature refrigeration systems and hot water heat pumps. Due to its low critical temperature of 31.1°C and high critical pressure of 73.8 bar relative to conventional refrigerants, CO₂ is utilized at much higher operating pressures, conditions at which the extrapolation of conventional flow pattern maps and flow boiling models does not work. In fact, the higher operating pressures result in much higher vapor densities and vapor viscosities and much lower surface tensions and liquid viscosities, thus yielding flow boiling heat transfer and two-phase flow characteristics that are quite different from those of conventional refrigerants. In particular, CO₂ has much larger nucleate boiling heat transfer coefficients than conventional refrigerants at the same saturation temperature and, as a consequence, its nucleate boiling coefficients are often much larger than their corresponding convective heat transfer coefficients, which is the inverse of the situation for conventional refrigerants. In addition, previous experimental studies have demonstrated that the onset of dryout tends to occur earlier for CO₂ flow boiling (it begins at lower vapor qualities). Significant discrepancies between flow patterns observed for CO₂ compared with the flow pattern maps that were developed for other fluids at lower pressures have been observed as well.

Thome and Ribatski (2006) have recently reviewed the CO₂ flow boiling heat transfer and two-phase flow literature. Their review addressed the experimental studies on heat transfer and two-phase flow in macro-channels and micro-channels, macro- and micro-scale heat transfer prediction methods for CO₂ and comparisons of these methods to an experimental database extracted from the same literature. In addition, the study of CO₂ two-phase flow patterns were summarized and compared to some of the leading flow pattern maps. Taking into account the lack of a well-established criterion to identify macro and micro-scale channels, they arbitrarily adopted a diameter of 3 mm to segregate the databases and heat transfer models into macro-channels and micro-channels. They found that the CO₂ prediction methods by Wang et al. (2003), Yoon et al. (2003) and Yoon et al. (2004) failed to predict most of the macro-channel experimental data while the CO₂ method proposed by Thome and El Hajal (2004) predicted reasonably well the newer macro-scale database of CO₂ only at low vapor qualities. They also found that both micro-scale and macro-scale prediction methods performed poorly when compared against independent small diameter data.

In response, Cheng et al. (2006) have proposed an updated flow pattern map and flow boiling model for CO₂ that will be described here in this keynote lecture. The details of the experimental conditions of the CO₂ flow boiling database covered by their study are summarized in their paper. It includes experimental results from six independent studies obtained for mass velocities from 80 to 570 kg/m²s, heat fluxes from 5 to 32.06 kW/m², saturation temperatures from -28 to 25°C (the corresponding reduced pressures are from 0.21 to 0.87) and tube diameters from 0.8 to 10.06 mm. All those experiments were conducted in horizontal tubes. Refer to their paper for a detailed description of the selection of studies chosen for their database.

In Cheng et al. (2006), a new general heat transfer model and a new flow pattern map physically related to the heat transfer mechanisms were developed specially for CO₂. As the starting point, the model developed by Wojtan et al. (2005a, 2005b) was used, which is an updated version of the flow pattern maps and flow boiling heat transfer models of

Kattan et al. (1998a, 1998b) and Thome and El Hajal (2004). The new proposed prediction method includes new correlations for the nucleate boiling heat transfer and the suppression factor based on CO₂ experimental data. In addition, a new dryout inception vapor quality correlation was proposed for CO₂ and accordingly the heat transfer predictions in the dryout region were improved by better identification of this regime's boundary. Based on the heat transfer data and its sharp changes in trends, a new flow patterns map was proposed and thus can physically explain the heat transfer phenomena according to the flow regimes defined by the new flow map.

2. New Cheng-Ribatski-Wojtan-Thome CO₂ flow pattern map

The new flow pattern map for CO₂ of Cheng et al. (2006) was developed according to the corresponding heat transfer mechanisms in various flow regimes. Based on their heat transfer database (not flow pattern observations that are quite limited for CO₂), the intermittent flow to annular flow transition (I-A) and the annular flow to dryout region transition (A-D) criteria in the flow pattern map of Wojtan et al. (2005a) were modified to fit the experimental data of CO₂. Thus, their new flow pattern map is directly related to the corresponding heat transfer mechanisms and trends of CO₂. The other transition criteria remained the same as in Wojtan et al. (2005a) and are not discussed further here.

To reflect the real mass flow velocities for non-circular channels, *equivalent diameters* are used for non-circular channels rather than hydraulic diameters, the latter which seem to have no physical relationship to an annular film flow for instance. The equivalent diameter is that of a circular channel with the same cross-sectional area as the non-circular channel, such that the mass velocities remain the same in both channels (this is not true when using the hydraulic diameter). Furthermore, when using a void fraction equation to calculate mean velocities of the phases, these remain the same in an equivalent diameter tube as in the non-circular tube but not in a hydraulic diameter tube.

Flow pattern transitions under diabatic flow boiling conditions are, in part, intrinsically related to the changes in trends in flow boiling heat transfer coefficients. This means that flow pattern maps can be used to explain the characteristics of flow boiling data and vice versa. Specifically in the present case, CO₂ depicts strong nucleate boiling heat transfer characteristics in intermittent flow at low vapor quality due to its high reduced pressure. The distinction between intermittent (I) flow and annular (A) flow was indicated by the sharp decline of the heat transfer coefficient data between the two flow regimes. The entrance into the dryout region (D) is also quite evident by the sharp drop in heat transfer when the top of a horizontal tube becomes dry, where the fraction of the perimeter then grows with increasing vapor quality until the entire perimeter is dry and mist flow is encountered, with yet another characteristic change in trend in the heat transfer data. Therefore, the distinction between annular flow and dryout region was determined by analysis of the heat transfer database.

Based on the experimental heat transfer data, the following new transition criteria were proposed for CO₂:

1. The I-A transition boundary was calculated with its new criterion as follows:

$$x_{IA} = \left[1.8^{1/0.875} (\rho_V / \rho_L)^{-1/1.75} (\mu_L / \mu_V)^{-1/7} + 1 \right]^{-1} \quad (1)$$

2. The A-D transition boundary was calculated with its new criterion as follows:

$$G_{dryout} = \left\{ \frac{1}{0.67} \left[\ln \left(\frac{0.58}{x} \right) + 0.52 \left[\frac{D}{\rho_V \sigma} \right]^{-0.17} \left[\frac{1}{g D \rho_V (\rho_L - \rho_V)} \right]^{-0.348} \left(\frac{\rho_V}{\rho_L} \right)^{-0.25} \left(\frac{q}{q_{crit}} \right)^{-0.7} \right] \right\}^{0.965} \quad (2)$$

The new onset of dryout inception vapor quality x_{di} that marks the transition from annular flow to dryout is predicted as:

$$x_{di} = 0.58 e^{\left[0.52 - 0.67 W_{eV}^{0.17} Fr_V^{0.348} (\rho_V / \rho_L)^{0.25} (q / q_{crit})^{0.7} \right]} \quad (3)$$

In this equation, q_{crit} is calculated according to Kutateladze (1948). For non-circular channels, equivalent diameters are used for non-circular channels in the flow pattern map.

Figure (1, top) shows the comparison of the new flow pattern map for CO₂ and the flow pattern map of Wojtan et al. to the experimental data of Yun et al. (2005) at the indicated test conditions. In the flow pattern map, A stands for annular flow, D stands for the dryout region, I stands for intermittent flow, M stands for mist flow, S stands for stratified flow and SW stands for stratified-wavy flow. The stratified to stratified-wavy flow transition is designated as S-SW, the stratified-wavy to intermittent/annular flow transition is designated as SW-I/A, the intermittent to annular flow transition is designated as I-A and so on. The arrows show the changes of I-A, A-D and S-SW/Slug+SW transition boundaries made for CO₂. Figure (1, bottom) shows the corresponding comparison of the predicted heat transfer coefficients with the heat transfer model of Wojtan et al. and the new heat transfer model (described below) for CO₂ to the experimental data at the same conditions. Obviously, the flow pattern map of Wojtan et al. did not reflect the sharp changes in trends in CO₂ heat transfer correctly and the heat transfer model for conventional refrigerants of Wojtan et

al. predicted poorly the experimental heat transfer coefficients of CO₂. The new CO₂ flow pattern map thus helps the flow boiling heat transfer model to capture the location of the sharp fall off in heat transfer and thus increase both the accuracy and reliability of the new heat transfer model.

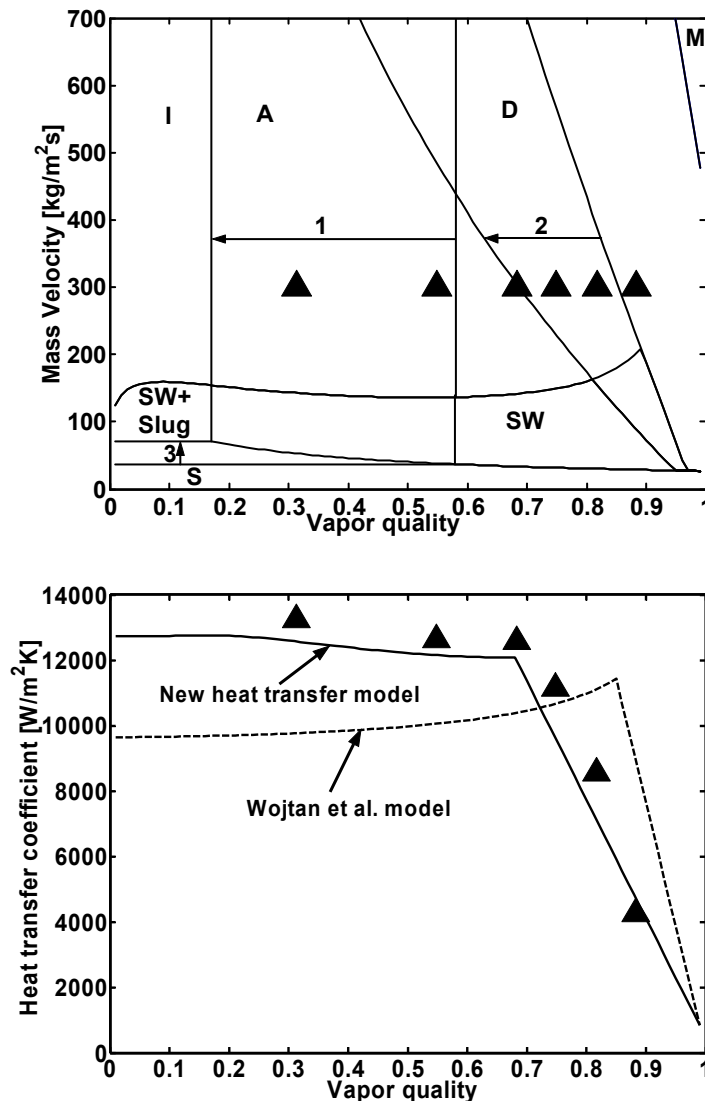


Figure 1. New flow pattern map (top) and heat transfer data (bottom) of Yun et al. (2005) for CO₂ for $D = 1.54$ mm, $G = 300$ kg/m²s, $T_{sat} = 5$ °C and $q = 20$ kW/m². Arrow 1 shows the change of I-A transition boundary, arrow 2 the change of A-D transition boundary and arrow 3 the change of S-SW/Slug-SW+ boundary.

3. New Cheng-Ribatski-Wojtan-Thome flow boiling heat transfer model for CO₂

It was a formidable challenge to develop a general flow boiling heat transfer model for CO₂ because of the significant diversities of the heat transfer trends in the database from study to study. Furthermore, since such a method will be used to optimize the configuration and size of CO₂ evaporators, it is important that it is not only statistically accurate but that it captures correctly the trends in the data and in particular the locations of the sharp changes in heat transfer. Most importantly, the heat transfer mechanisms should be related to the corresponding flow patterns and be physically explained according to flow pattern transitions. Accordingly, Cheng et al. (2006) proposed a new general heat transfer model for CO₂ using the Wojtan et al. (2005b) model as the starting point. Equivalent diameters are used for non-circular channels in the heat transfer model.

3.1. Brief description of the flow boiling heat transfer model of Wojtan et al.

Wojtan et al. (2005b) extended the Kattan et al. (1998b) heat transfer model to include a dryout region and heat transfer methods for the dryout and mist flow regimes and improved the heat transfer predictions for stratified-wavy flows by dividing that regime into three sub-regimes. The Kattan-Thome-Favrat general equation for the local heat transfer coefficients h_{tp} in a horizontal tube is:

$$h_{ip} = [\theta_{dry} h_V + (2\pi - \theta_{dry}) h_{wet}] / 2\pi \quad (4)$$

where θ_{dry} is the dry angle as shown in Figure (2). The dry angle is used in defining the basic two-phase flow structures and the ratio of the tube perimeters in contact with liquid and vapor. In stratified flow, θ_{dry} equals the stratified angle, θ_{strat} , which is calculated according to the method in Thome and El Hajal (2004). In annular and intermittent flows, $\theta_{dry} = 0$. For stratified-wavy flow, θ_{dry} varies from zero up to its maximum value θ_{strat} . Wojtan et al. subdivided the stratified-wavy flow into three subzones (slug, slug/stratified-wavy and stratified-wavy). Based on the fact that the high frequency slugs maintain a continuous thin liquid layer on the upper tube perimeter, θ_{dry} is defined equal to 0 in the slug zone. The dry angles in the slug/stratified-wavy and stratified-wavy regions are calculated according to equations developed by Wojtan et al. based in exponential interpolations giving smooth transition in the determination of the dry angle between the respective zones and also a smooth transition in the heat transfer coefficient from zone to zone.

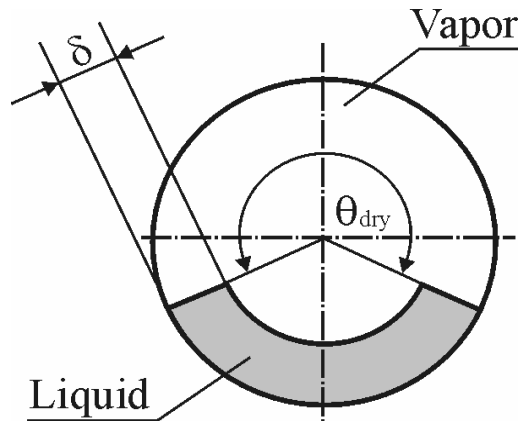


Figure 2. Schematic diagram of annular flow with partial dryout.

The vapor phase heat transfer coefficient on the dry perimeter h_V is calculated with the Dittus-Boelter (1930) correlation assuming tubular flow in the tube:

$$h_V = 0.023 Re_V^{0.8} Pr_V^{0.4} (k_V / D) \quad (5)$$

and the heat transfer coefficient on the wet perimeter is calculated with an asymptotic model that combines the nucleate boiling and convective boiling contributions to the heat transfer by the third power:

$$h_{wet} = [(h_{nb})^3 + h_{cb}^3]^{1/3} \quad (6)$$

In this equation, the correlation proposed by Cooper (1984) multiplied by a fixed boiling suppression factor of 0.8 was used to calculate the nucleate boiling contribution. The convective contribution was calculated as in the original Kattan et al. correlation assuming a liquid film flow:

$$h_{cb} = 0.0133 \left(\frac{4G(1-x)\delta}{\mu_L(1-\varepsilon)} \right)^{0.69} Pr_L^{0.4} \frac{k_L}{\delta} \quad (7)$$

The term in the bracket is the liquid film Reynolds number. The void fraction ε is determined with the Rouhani and Axelsson (1970) drift flux model and the liquid film thickness from the geometry in Fig. (2) as in Wojtan et al.

The heat transfer coefficient in mist flow is calculated as follows in the Wojtan et al. model:

$$h_{mist} = 0.0117 Re_H^{0.79} Pr_V^{1.06} Y^{-1.83} (k_V / D) \quad (8)$$

where Re_H is the homogeneous Reynolds number and Y is the correction factor originally proposed by Groeneveld (1973) and given by:

$$Y = 1 - 0.1 [(\rho_L / \rho_V - 1)(1-x)]^{0.4} \quad (9)$$

The heat transfer coefficient in the dryout region along a horizontal channel is calculated by proration as:

$$h_{dryout} = h_{tp}(x_{di}) - \frac{x - x_{di}}{x_{de} - x_{di}} [h_{tp}(x_{di}) - h_{mist}(x_{de})] \quad (10)$$

In this expression, $h_{tp}(x_{di})$ is the two-phase flow heat transfer coefficient calculated from Eq. (4) at the dryout inception quality x_{di} and $h_{mist}(x_{de})$ is the mist flow heat transfer coefficient calculated from Eq. (8) at the dryout completion quality x_{de} . If x_{de} is calculated to be larger than 0.999, then x_{de} is reset to 0.999. For more details and complete set of equations for the flow boiling heat transfer model and flow patterns map of Wojtan et al., refer to the original papers.

3.2. Modifications in the new flow boiling heat transfer model for CO₂

Like other flow boiling heat transfer models, both the original Kattan-Thome-Favrat model and the modified model of Wojtan et al. significantly underpredict the flow boiling heat transfer coefficients for CO₂, particularly at low and intermediate vapor qualities. Interestingly, CO₂ heat transfer data at high saturation pressures typically show a monotonic decrease versus vapor quality in annular flows, which is the exact opposite of the trend for other refrigerants such as R134a at low pressures. The nucleate boiling contribution is much larger than the convective boiling contribution for CO₂ while the opposite is true for R-134a. Hence, the suppression of nucleate boiling that could be neglected in the asymptotic method for conventional refrigerants at low pressures cannot be neglected for CO₂, where suppression of nucleate boiling greatly reduces its contribution to the heat transfer with increasing vapor quality.

Therefore, first Cheng et al. (2006) developed a new nucleate boiling heat transfer correlation, found to be necessary for CO₂, and then a new boiling suppression factor S was proposed for CO₂. Furthermore, a new correlation for the onset of dryout inception was needed and is given by Eq. (3), in order to predict heat transfer in the dryout region by considering the fact that the onset of dryout of CO₂ occurs much earlier than for other refrigerants.

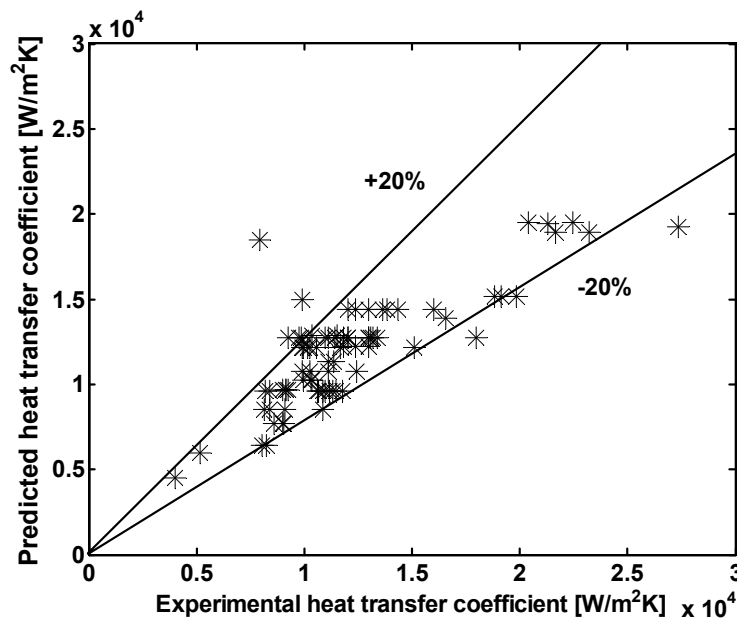


Figure 3. Comparison of their nucleate boiling heat transfer correlation for CO₂ with their database.

Nucleate boiling heat transfer correlation for CO₂. The experimental flow boiling heat transfer data at vapor qualities $x < x_{LI}$ in the CO₂ database were used to extract the nucleate boiling contribution by removing their convective heat transfer contributions using the above equations to develop a nucleate boiling database for CO₂. The Cooper (1984) correlation was found to greatly under predict these data at low heat fluxes while the correlation of Gorenflo (1993) over predicted the data by a large margin, where the reason could be the lack of an extensive database for pool boiling of CO₂ in setting his standardized value for CO₂. Thus, the following new nucleate boiling heat transfer correlation for CO₂ was proposed by Cheng et al.:

$$h_{nb} = 131 p_r^{-0.0063} (-\log_{10} p_r)^{-0.55} M^{-0.5} q^{0.58} \quad (11)$$

Figure (3) shows the comparison of these “nucleate boiling heat transfer coefficients” by the new nucleate boiling heat transfer correlation for CO₂, where about 90% of the data are predicted within ± 20%.

Nucleate boiling suppression factor correlation for CO₂. As nucleate boiling heat transfer is suppressed by the sharper temperature gradient in the liquid film in an annular flow as per the theory of Chen (1966), a boiling suppression factor correlation is needed in the flow boiling heat transfer model for CO₂ to capture the effect. Unlike other earlier boiling suppression factor correlations, which were empirically correlated based on the Lockhart-Martinelli number, Reynolds number, Boiling number and Prandtl number, the liquid film thickness was used as a main parameter by Cheng et al. since it was found by analysis of their data to have a significant effect on the values of S back-calculated out of their flow boiling database as follows. First, the Cooper correlation was first replaced with the new nucleate boiling heat transfer correlation. Then, the boiling suppression factors were backed out of the whole database (except the dryout data points) using the above expressions. Incorporating the effect of tube diameter, the following boiling suppression factor correlation was obtained for CO₂:

$$\text{If } x < x_{IA}$$

$$S = 1 \tag{12}$$

$$\text{If } x \geq x_{IA},$$

$$S = 1 - 1.14 \left(D/D_{ref} \right)^2 \left(1 - \delta/\delta_{IA} \right)^{2.2} \tag{13}$$

where $D_{ref}=0.00753\text{m}$. Furthermore, if $D > 7.53 \text{ mm}$, then set $D = 7.53 \text{ mm}$. For non-circular channels, the equivalent diameter is used. The correlation is applicable to the conditions: $-28^\circ\text{C} \leq T_{sat} \leq 25^\circ\text{C}$, $5 \text{ kW/m}^2 \leq q \leq 32 \text{ kW/m}^2$, $170 \text{ kg/m}^2\text{s} \leq G \leq 570 \text{ kg/m}^2\text{s}$, $0.8 \text{ mm} \leq D \leq 10 \text{ mm}$.

Combining the nucleate boiling heat transfer correlation for CO₂ and the nucleate boiling heat transfer suppression factor correlation, the flow boiling heat transfer coefficients on the wet perimeter are now calculated as:

$$h_{wet} = \left[(S \cdot h_{nb})^3 + h_{cb}^3 \right]^{1/3} \tag{14}$$

Dryout region heat transfer correlation for CO₂. When developing their boiling suppression factor correlation, dryout data were determined according to the corresponding boiling suppression factors. Those giving negative boiling suppression factor values were taken as the dryout points and the data giving boiling suppression factor values around zero were taken as indicating the onset of the dryout. Based on these dryout inception data, the dryout inception vapor quality correlation of Wojtan et al. was modified and thus a new annular to dryout region (A-D) transition boundary in the flow pattern map was extracted for CO₂. By comparing the new flow pattern map with the experimental data, the dryout inception vapor quality correlation was modified and is given by Eqs. (2) and (3) presented earlier.

3.3. Comparisons of the new flow boiling heat transfer model to the database

Figures (4) and (5) show their comparisons of the new flow boiling heat transfer model to a selection of experimental heat transfer coefficients. Generally, the new heat transfer model predicts the experimental heat transfer coefficients well and captures the trends of the experimental heat transfer coefficients. The statistical analysis found that 75.5% of the entire database was predicted within ± 30% using the new Cheng et al. flow pattern map and flow boiling model for CO₂. For such a wide range of experimental data from different laboratories, especially covering data in the dryout, mist and stratified-wavy flow regimes, the predicted results are quite reasonable and encouraging.

As even more CO₂ data have become available since the work on Cheng et al. (2006) study was completed in 2005, Thome and coworkers are implementing further improvements to the methods presented here and hope to have an even more accurate, more reliable method that covers a larger range of test conditions available in 2007.

Figure (6) shows a simulation of the new flow pattern map and flow boiling model for CO₂ calculated for a 7 mm channel at a heat flux of 10 kW/m², a saturation temperature of -20°C and a mass velocity of 400 kg/m²s, superimposed on the same graph using the calculator embedded within the newest version of the e-book of Thome (2006). The process path for the vapor quality variation from $x = 0.01$ to $x = 0.99$ is shown as the broken red line while the variation in the heat transfer coefficient as it changes vapor quality and flow pattern is depicted by the solid red line. The flow pattern boundaries are in black. Notice the various changes in trends in the heat transfer coefficient as this occurs. For example, when the flow regime passes from annular flow into the dryout regime there is a sharp inflection in the heat transfer coefficient as the top perimeter of the tube becomes dry.

Figure (7) similarly depicts another simulation for a 7 mm channel at the following conditions: $q = 5 \text{ kW/m}^2$, $T_{sat} = 10^\circ\text{C}$ and $G = 200 \text{ kg/m}^2\text{s}$. It can be noticed that at this condition that the slug flow regime disappears (the black curved

line within the slug+SW region is the continuation of the G_{wavy} transition line, which is below the horizontal upper boundary of this latter regime and hence the slug regime does not appear in the map).

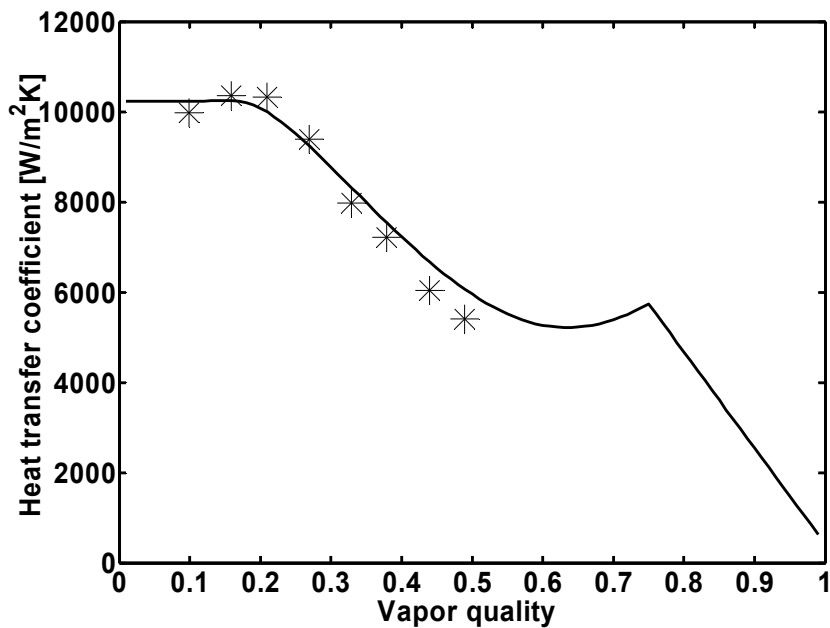


Figure 4. Comparison of the predicted flow boiling heat transfer coefficients with the experimental flow boiling heat transfer coefficients of Yoon et al. (2004) for $D=7.35$ mm, $T_{sat}=0$ °C, $G=318$ kg/m²s, $q=16.4$ kW/m².

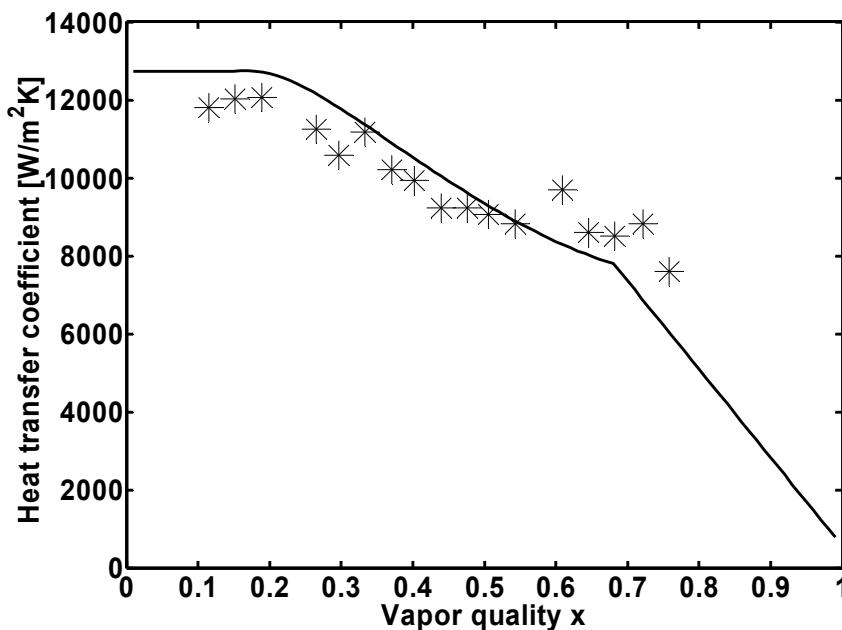


Figure 5. Comparison of the predicted flow boiling heat transfer coefficients with the experimental flow boiling heat transfer coefficients of Yun et al. (2003) for $D=6$ mm, $T_{sat}=5$ °C, $G=340$ kg/m²s, $q=20$ kW/m².

4. Conclusions

This keynote lecture has described the new flow boiling heat transfer model and a new flow pattern map for two-phase flow in horizontal tubes that has been developed specifically for CO₂ by Cheng et al. (2006). The new flow boiling heat transfer model and map include a new nucleate boiling heat transfer correlation for CO₂, a new nucleate boiling suppression factor correlation for CO₂ and a new dryout inception vapor quality correlation for CO₂. The new heat transfer model predicts 75.5% of the CO₂ database (318 data points) to within $\pm 30\%$ and 79.1% of the CO₂ database (287) without dryout data points. The heat transfer model and the corresponding flow pattern map are applicable to quite a wide range of conditions: tube diameters (equivalent diameter for non-circular channels) from 0.8 to 10 mm, mass velocities from 170 to 570 kg/m²s, heat fluxes from 5 to 32 kW/m² and saturation temperatures from -25°C to $+25^{\circ}\text{C}$.

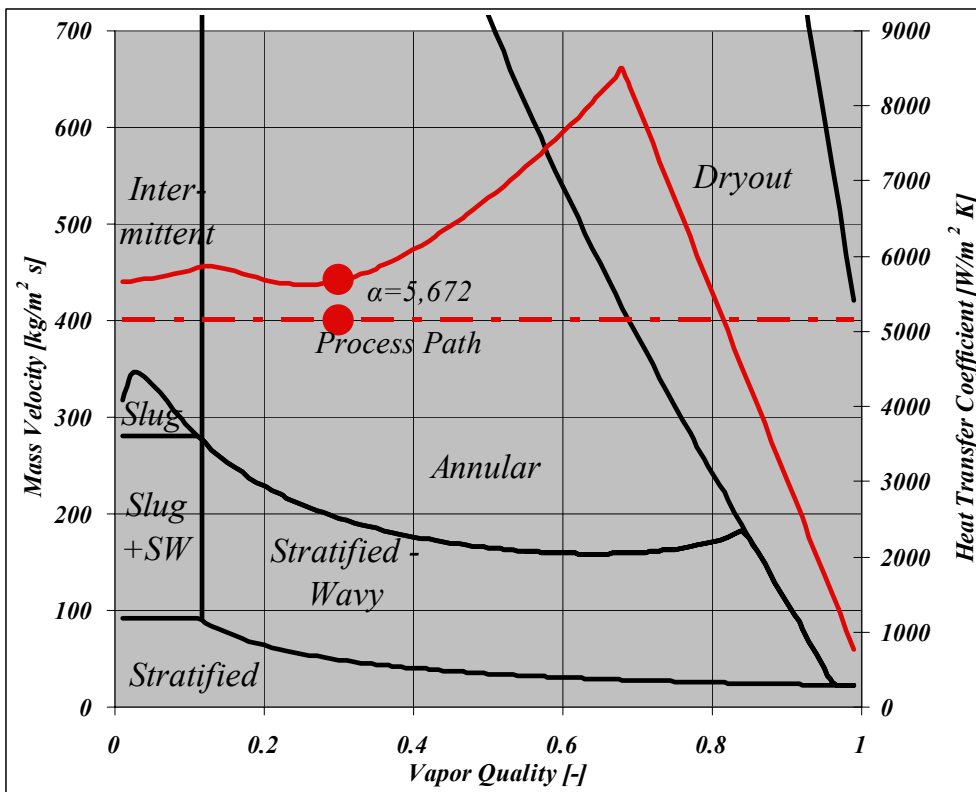


Figure 6. Simulation of flow boiling model and flow pattern map for 7 mm channel at following conditions: $q = 10 \text{ kW/m}^2$, T_{sat} at -20°C and $G = 400 \text{ kg/m}^2\text{s}$ with indicated value at $x = 0.30$.

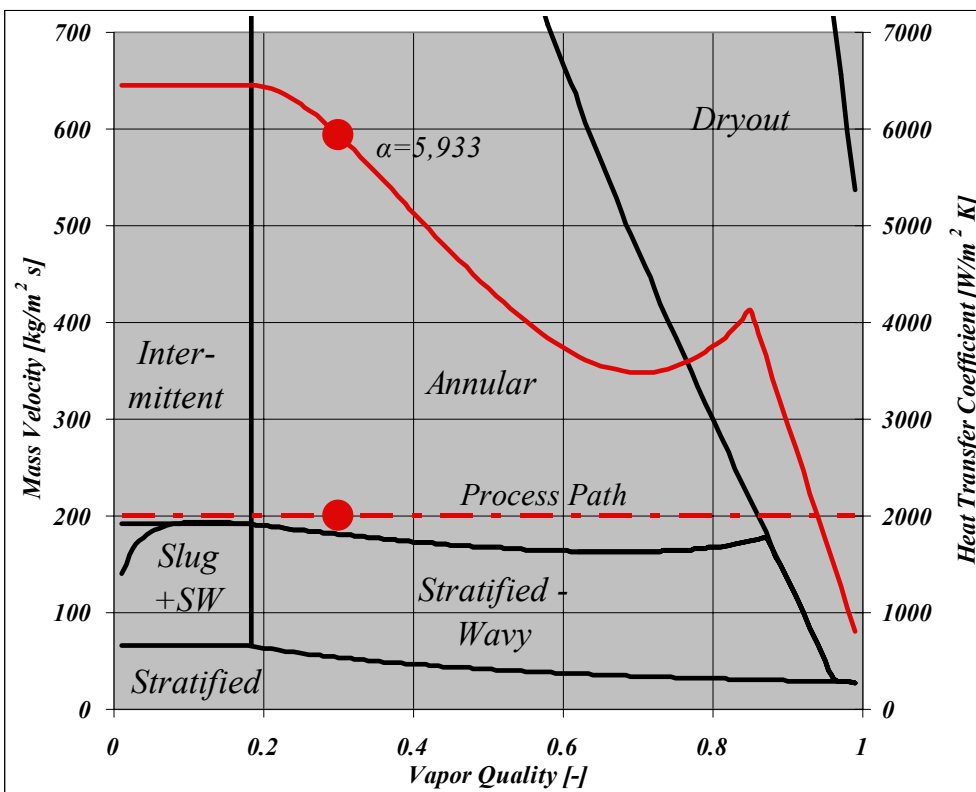


Figure 7. Simulation of flow boiling model and flow pattern map for 7 mm channel at following conditions: 5 kW/m^2 , T_{sat} at 10°C and $G = 200 \text{ kg/m}^2\text{s}$ with indicated value at $x = 0.30$.

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