



ECONOMIC DISPATCH OPTIMIZATION OF THERMAL UNITS BASED ON A MODIFIED FIREFLY ALGORITHM

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Abstract. *The objective of the economic dispatch problem (EDP) of electric power generation, whose characteristics are complex and highly nonlinear, is to schedule the committed generating unit outputs so as to meet the required load demand at minimum operating cost while satisfying all unit and system equality and inequality constraints. Recently, as an alternative to the conventional mathematical approaches, modern heuristic optimization techniques have been given much attention by many researchers due to their ability to find an almost global optimal solution in EDPs. This paper proposed a modified firefly algorithm (MFA) based on situational knowledge applied to EDPs. The FA is a stochastic metaheuristic approach based on the idealized behavior of the flashing characteristics of fireflies. In FA, the flashing light can be formulated in such a way that it is associated with the objective function to be optimized, which makes it possible to formulate the firefly algorithm. A classical FA and the MFA are validated for a test system consisting of a 13 thermal units whose incremental fuel cost function takes into account the valve-point loading effects. Furthermore, the obtained results are compared with results presented in the literature.*

Keywords: thermal units, economic dispatch, optimization, metaheuristics, firefly algorithm.

1. INTRODUCTION

Power utilities are expected to generate electrical power at minimum cost within the generator and system limits. Economic dispatch (ED) plays a major role in this aspect (Wood and Wollenberg, 1996). The basic objective of ED problem is to schedule the committed generating units to meet the system load demand at minimum operating cost while satisfying the various system equality and inequality constraints (Sivasubramani and Swarup, 2011).

Bio-inspired metaheuristics such as genetic algorithm (Walters and Sheblé, 1993), evolutionary programming (Sinha et al., 2003), differential evolution (Noman and Iba, 2008), cultural differential evolution (Coelho et al., 2008), ant colony (Pothiya et al., 2010), bacterial foraging (Saber, 2012), honey bee mating (Niknam et al., 2011), and particle swarm optimization (Panigrahi et al., 2008) have been used to solve ED optimization problem.

Recently, a new metaheuristic algorithm called firefly algorithm (FA) was proposed. FA is a new population-based metaheuristic approach developed by Xin-She Yang (Yang, 2008; Yang, 2009), which is nature-inspired by the behavior of the flashing characteristics of fireflies. In this context, the flashing light can be formulated in such a way that it is associated with the objective function to be optimized, which makes it possible to formulate the firefly algorithm.

In this paper, we present a modified FA (MFA) based on the situational knowledge source (memories of successful solutions). This kind of knowledge is usual in cultural algorithms (Reynolds, 1994). An economic dispatch problem is employed to demonstrate the performance of the FA and IFA approaches. In this context, a 13-unit test system (Sinha et al., 2003) with incremental fuel cost function taking into account the valve-point loading effects is used to illustrate the effectiveness of the FA and the proposed IFA. Simulation results obtained with the FA and IFA approaches were analyzed and compared with other optimization results reported in the literature.

The remainder of this paper is organized as follows: Section 2 describes the formulation of the ED optimization problem, while Section 3 explains the fundamentals of FA and IFA. After, Section 4 presents the simulation results for a test system with 13 thermal units. Finally, the conclusion and further research are discussed in Section 5.

2. FUNDAMENTALS OF ECONOMIC DISPATCH OPTIMIZATION PROBLEM

The primary concern of an economic dispatch problem is to minimize the total fuel cost at thermal power plants subjected to the operating constraints of a power system. Therefore, it can be formulated mathematically with an objective function and two constraints. The equality and inequality constraints are represented by equations (1) and (2) given by (Vianna Neto et al., 2009):

$$\sum_{i=1}^n P_i - P_L - P_D = 0 \quad (1)$$

$$P_i^{\min} \leq P_i \leq P_i^{\max} \quad (2)$$

In the power balance criterion, an equality constraint must be satisfied, as shown in equation (1). The generated power should be the same as the total load demand plus total line losses. The generating power of each generator should lie between maximum and minimum limits represented by equation (2), where P_i is the power of generator i (in MW); n is the number of generators in the system; P_D is the system's total demand (in MW); P_L represents the total line losses (in MW) and P_i^{\min} and P_i^{\max} are, respectively, the output of the minimum and maximum operation of the generating unit i (in MW) (Vianna Neto et al., 2009). The objective of minimization of the total fuel cost function is formulated as follows:

$$\min f = \sum_{i=1}^n F_i(P_i) \quad (3)$$

where F_i is the total fuel cost for the generator unit i (in \$/h), which is defined by equation:

$$F_i(P_i) = a_i P_i^2 + b_i P_i + c_i \quad (4)$$

where a_i , b_i and c_i are cost coefficients of generator i .

The sequential valve-opening process for multi-valve steam turbines produces ripple like effect in the heat rate curve of the generator. This effect is included in economic dispatch problem by superimposing the basic quadratic fuel-cost characteristics with a rectified sinusoidal component. In this context, the equation (4) can be modified as (Vianna Neto et al., 2009):

$$\tilde{F}_i(P_i) = F_i(P_i) + \left| e_i \sin\left(f_i \left(P_i^{\min} - P_i\right)\right) \right| \quad \text{or} \quad (5)$$

$$\tilde{F}_i(P_i) = a_i P_i^2 + b_i P_i + c_i + \left| e_i \sin\left(f_i \left(P_i^{\min} - P_i\right)\right) \right| \quad (6)$$

where e_i and f_i are valve-point loading coefficients of generator i . Hence, the total fuel cost that must be minimized, according to equation (3), is modified to:

$$\min f = \sum_{i=1}^n \tilde{F}_i(P_i) \quad (7)$$

where \tilde{F}_i is the cost function of generator i (in \$/h) defined by equation (6). In the case study presented here, we disregarded the transmission losses, P_L (mentioned in equation (1)), i.e., in this work $P_L = 0$.

3. FIREFLY ALGORITHM

This section describes the proposed FA. First, a brief overview of the FA is provided, and finally the modification procedures of the proposed MFA are presented.

3.1 Classical firefly algorithm

The FA is a metaheuristic algorithm, inspired by the flashing behavior of fireflies. As a firefly's attractiveness is proportional to the light intensity seen by adjacent fireflies, we can now define the attractiveness β of a firefly in terms of Cartesian distance between firefly i and firefly j . In this case, the movement of a firefly i is attracted to another more attractive (brighter) firefly j is determined by (Yang, 2008)

$$x_i = x_i + \beta_0 e^{-\gamma r_{ij}^2} (x_j - x_i) + \alpha \left(rand - \frac{1}{2} \right) \quad (8)$$

where the second term is due to the attraction, where γ is the absorption coefficient, and β_0 is the attractiveness at $r = 0$. The third term is related to randomization factor with α being the randomization parameter. The value of $rand$ is a random number generator uniformly distributed in $[0, 1]$. The procedure for implementing the FA can be summarized as the pseudocode (adapted of Yang (2008) and Yang (2009)) shown in Fig. 1.

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Objective function of optimization problem  $f(x)$ ,  $x = (x_1, \dots, x_d)^T$ 
Generate initial population of  $n$  fireflies  $x_i$  ( $i = 1, 2, \dots, n$ ) using generation of numbers with uniform distribution
Light intensity  $I_i$  at  $x_i$  is determined by  $f(x_i)$ 
Define light absorption coefficient  $\gamma$ 
Initial generation,  $k = 0$ 

while ( $k < Maximum\_Generations$ )
  Update the generation number,  $k = k + 1$ 
  for  $i = 1$  to  $n$  (all  $n$  fireflies)
    for  $j = 1$  to  $i$  (all  $n$  fireflies)
      if ( $I_j < I_i$ ) in case of a minimization problem
        Move firefly  $i$  towards  $j$  in  $d$ -dimension;
      end if
      Attractiveness varies with distance  $r$  via equation (8)
      Evaluate new solutions and update light intensity
    end for  $j$ 
  end for  $i$ 
  Rank the fireflies and find the current best
end while
Postprocess results and visualization

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Figure 1. Pseudocode of the FA.

3.2 Modified firefly algorithm

The MFA employs a situational knowledge source, which changes the movement equation (8). This source stores the best firefly along the iterations, that is performed by changing the situational knowledge firefly E to x_i , at each iteration, if x_i is feasible.

Becerra and Coello (2006) proposed a cultured differential evolution (CDE), in which MFA situational knowledge was based. The new equation (9), which replaces equation (8), is the adapted form from the CDE to the firefly algorithm, where x_j moves toward E , instead of x_i towards x_j . It provides a better algorithm's convergence.

$$x_i = x_j + a * \beta_0 e^{\gamma r_{ij}^2} (E - x_j) + b\alpha \left(rand - \frac{1}{2} \right) \quad \text{where} \quad (9)$$

$$a = \frac{F(x_j) - F(E)}{\max(F(x)) - \min(F(x))} \quad \text{and} \quad (10)$$

$$b = \max(x) - \min(x) \quad (11)$$

The new equation has two new terms, a and b , each one described by equations (10) and (11), respectively. The term a associates firefly's light weighing to the movement, making the step proportional to the light difference. While b guides the random movement, updating MFA's range and this procedure can be useful to avoid performance losses. The $\max(x)$ and $\min(x)$ are the maximum and minimum values of the x -vector.

4. DESCRIPTION OF THE TEST SYSTEM AND SIMULATION RESULTS

This case study consisted of 13 thermal units of generation with the effects of valve-point loading, as given in Table 1. The data shown in Table 1 are also available in Sinha et al. (2003). In this case, it adopted a load demand to be determined, P_D , equal to 1800 MW.

Table 1. Data for the 13 thermal units of the test system.

Thermal unit	P_i^{\min}	P_i^{\max}	a	b	c	e	f
1	0	680	0.00028	8.10	550	300	0.035
2	0	360	0.00056	8.10	309	200	0.042
3	0	360	0.00056	8.10	307	150	0.042
4	60	180	0.00324	7.74	240	150	0.063
5	60	180	0.00324	7.74	240	150	0.063
6	60	180	0.00324	7.74	240	150	0.063
7	60	180	0.00324	7.74	240	150	0.063
8	60	180	0.00324	7.74	240	150	0.063
9	60	180	0.00324	7.74	240	150	0.063
10	40	120	0.00284	8.60	126	100	0.084
11	40	120	0.00284	8.60	126	100	0.084
12	55	120	0.00284	8.60	126	100	0.084
13	55	120	0.00284	8.60	126	100	0.084

The optimization methods were implemented in Matlab (MathWorks). In each case study, 30 independent runs were made for each of the optimization algorithms involving 30 different initial trial solutions for each optimization method. In all optimization approaches were adopted a population of n fireflies equal to 20 and *Maximum_Generations* = 100. A total of 2,000 cost function evaluations in each run were performed by tested FA approaches. Furthermore, the following setups were also adopted:

- FA: $\gamma = 1$, $\beta_0 = 1$ and $\alpha = 0.8$;
- Gaussian FA (GFA): $\gamma = 1$, $\beta_0 = 1$ and α is obtained with absolute values from a truncated normal distribution with mean equal to zero and unit standard deviation. In the Matlab implementation, it is given by $\alpha = \text{abs}(\text{randn})/3.5$;
- MFA(1): $\gamma = 1$, $\beta_0 = 1$ and $\alpha = 0.8$;
- MFA(2): $\gamma = 1$, $\beta_0 = 1$ and α is a random number generator uniformly distributed in $[0, 1]$;
- MFA(3): $\gamma = 1$, $\beta_0 = 1$ and α is given by same procedure adopted in the GFA.

A key factor in the application of optimization methods is how the algorithm handles the constraints relating to the problem. In this work, a penalty-based method proposed in Noman and Iba (2008) was used.

The results obtained for the test system are given in Table 2, which shows that the MFA succeeded in finding better solutions than the FA for the ED with load demand of 1800 MW. Furthermore, a lower standard deviation value indicated a good convergence of MFA method in the 30 runs.

Table 2. Convergence results (30 runs) for the test system with 13 thermal units with valve point.

Optimization Method	Minimum Cost (\$/h)	Mean Cost (\$/h)	Maximum Cost (\$/h)	Standard Deviation of Cost (\$/h)
FA	18685.6525	18938.5074	19094.1757	104.5127
GFA	18866.5697	18990.7972	19098.0051	68.6925
MFA(1)	18259.5242	18389.4410	18556.7491	67.7687
MFA(2)	18188.1687	18362.3008	18491.1524	81.1922
MFA(3)	17972.8177	17993.2278	18073.6082	33.3766

From Table 2, the mean of cost function found by MFA(3) for the 30 runs was better than the results of FA and GFA methods. The best solution obtained for the vector P_i , $i = 1, \dots, 13$ with MFA(3) with total minimum cost of 17972.8177 \$/h for $P_D = 1800$ MW are given in Table 3. Table 4 compares the results obtained in this paper using MFA(3) with those of other studies reported in the literature. Note that in this studied case, the best result reported, in terms of the fuel cost using MFA(3) is comparatively lower than several studies presented in the literature. Furthermore, the results presented in Chiang et al. (2005), Wang et al. (2007) and Vlachogiannis and Lee (2009) are superior than the obtained by MFA(3).

Table 3. Best result (30 runs) for the test system using MFA(3).

Power	Generation (MW)
P_1	628.3185
P_2	297.6200
P_3	224.3283
P_4	60.0000
P_5	109.8665
P_6	60.0000
P_7	109.8665
P_8	60.0000
P_9	60.0000
P_{10}	40.0000
P_{11}	40.0000
P_{12}	55.0000
P_{13}	55.0000

Table 4. Comparison of results for the test system with the fuels costs presented in the literature.

Optimization technique	Best result in terms of the fuel cost (\$/h)
Improved evolutionary programming (Sinha et al., 2003)	17994.07
Hybrid genetic algorithm (Da-kuo et al., 2008)	17992.92
Particle swarm optimization (Victoire and Jeyakumar, 2004)	18030.72
Improved genetic algorithm (Chiang et al., 2005)	17963.98
Self-tuning hybrid differential evolution (Wang et al., 2007)	17963.79
Improved particle swarm optimization (Vlachogiannis and Lee, 2009)	17960.37
Best result of this paper using MFA(3)	17972.8177

5. CONCLUSION

Practical aspect like valve-point effects makes the solution space of ED optimization problem nonconvex with many local minima. It is extremely difficult to find the optimal solution for ED with multiple minima.

In order to demonstrate the performance and applicability of the proposed MFA method, a 13-unit test system with non-smooth fuel cost function is used. It has been observed that the MFA(3) has the ability to converge to a better quality near-optimal solution and possesses better convergence characteristics and robustness than other prevailing techniques reported in the literature. Future work will include a diversity measure of the fireflies' population in the MFA(3). Furthermore, we plan to study the MFA(3) in multiobjective ED problems with units having prohibited zones and valve-point loading effects.

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