# Hydraulic Power Plant Machine Dynamic Diagnosis

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Abstract. A method how to perform an entire structural and hydraulic diagnosis of prototype Francis power machines is presented and discussed in this report. Machine diagnosis of Francis units consists on a proper evaluation of acquired mechanical, thermal and hydraulic data obtained in different operating conditions of several rotary and non rotary machine components. Many different physical quantities of a Francis machine such as pressure, strains, vibration related data, water flow, air flow, position of regulating devices and displacements are measured in a synchronized way so that a relation of cause an effect can be developed for each operating condition and help one to understand all phenomena that are involved with such kind of machine. This amount of data needs to be adequately post processed in order to allow correct interpretation of the machine dynamics and finally these data must be compared with the expected calculated data not only to fine tuning the calculation methods but also to accomplish fully understanding of the influence of the water passages on such machines. The way how the power plant owner has to operate its Francis machines, many times also determined by a central dispatcher, has a high influence on the fatigue life time of the machine components. The diagnostic method presented in this report helps one to understand the importance of adequate operation to allow a low maintenance cost for the entire power plant. The method how to acquire these quantities is discussed in details together with the importance of correct sensor balancing, calibration and adequate correlation with the physical quantities. Typical results of the dynamic machine behavior, with adequate interpretation, obtained in recent measurement campaigns of some important hydraulic turbines were presented. The paper highlights the investigation focus of the hydraulic machine behavior and how to tailor the measurement strategy to accomplish all goals. Finally some typical recommendations based on the experience obtained on previous diagnostic reports of Francis turbines are performed in order to allow a better and safe operation of these power plant units.

Keywords: diagnosis, ,dynamic measurement, von Karman, power, Francis, frequency, speed no load, strain, stress.

## 1. Introduction

Francis hydraulic units are reaction machines that are designed according to specific hydraulic conditions limited by the hydrological variables such as head and the flow yearly variations. The hydro conditions of the power plant location will drive the Francis machine design and goals such as high efficiency unit operation and the maximum yearly unit utilization are pursued in order to increase the return of the investment.

This type of machine is designed according to computational fluid dynamics techniques and a scaled model is manufactured and tested on hydraulic laboratories to assure the design before the start of the real full scale machine prototype. The Hydraulic model test is also required because each machine is at the end tailored to specific hydro conditions that are rarely equal to any already existent one.

Although the turbine model test is suitable to understand the machine behavior at every loading condition from a hydraulic point of view, the full comprehension of the machine behavior and especially its structural response cannot be scaled up to prototype size according to the homology rules. The influence of the water intake inertia is something that can be checked only at prototype scale. There are some uncertainties that can be finally checked only at the prototype scale.

Added to this fact the structure mechanical response can hardly be evaluated on the model scale especially because the model runners are being manufactured in bronze which is much different than prototype runners that are typically performed in martensitic stainless steel inclusively with welded on buckets. The response of the components that are under water such as the stay vanes and the runner is particularly important because the flow will induce vibrations on those components and can be intense if adequate measures are not performed. Although one of the main design focus considers the goal of low dynamic stresses and low induced vibration, the nature of a fixed runner blade machine, such as Francis machines, will get some operating conditions suitable to rough dynamic loads and long term operation on that particular region might reduce the component life time at the highest stressed areas.

Due to the fact that Francis machines contain fixed blades, different from Kaplan units where another degree of freedom is added by the blade rotation that optimizes the blade inflow geometry according to the flow behavior, here the inflow angles are fixed and designed for some particular flow conditions. For intermediate load conditions the flow might get unstable. For a fixed head, the power changes according to changes in flow discharge that is regulated by the distributor wicket gate position that is, ultimately, driven by the electronic governor system. In order to establish the flow discharge the wicket gates rotate from an aligned position to a closed position. Since a Francis runner is typically a welded construction where the blades are attached to a crown and band, one unique blade geometry is defined for all operating loads even for a set of operating heads. This geometry is tailored to the rated or best efficiency region that is limited according to the design. By analyzing the tandem cascade that includes the stay vane, wicket gate and blade profile of a runner one can recognize that for one specific opening the water through the cascade will flow smoothly, "fig. 1". By closing the distributor the wicket gate blocks the flow and it is also possible to see that the flow streamline will change significantly from the best operating point condition, "fig. 2". This wicket gate intermediate position decreases the flow by incrementing the head loss but also generates flow swirls that pass through the runner inducing dynamic loads to the structure. The knowledge of amplitudes and frequencies of such dynamic loads is one of the goals of the proposed diagnosis. "Figure 3 & 4" show two sequences of the real flow behavior inside a model runner.



Fig.1 - Tandem Cascade -Best point





Fig.2-Tamdem Cascade intermediate opening

Fig.3 – Flow at Model Runner - Best point



The time to have a fatigue crack being initiated at the high stressed areas of a runner, for instance, is fully dependent of how the energy company or dispatcher operates the machine. If the operating condition considers the neighborhood of the rated machine point without many starts and stops the runner will probably have its maintenance costs driven to the lowest value. However if the machine is often operated at speed no load or any rough unstable condition with many starts and stops the chance to have cracks being initiated and to have considerable maintenance costs will be high.

The machine full diagnosis as described here will practically eliminate all prototype unknown variables and will provide the full comprehension of the machine behavior at every load condition. The generated data will allow one to get all fatigue related safety margins for each operating condition and shall allow the owner to optimize the operating conditions to reduce the possible change for high maintenance runner costs.

Occurrences of possible severe high frequency exciting phenomena will be discovered during the machine diagnosis and the cause will need to be eliminated in order to preserve the machine lifetime. Nevertheless occurrences of low frequency exciting loadings must be investigated in order to define and especially fine tune the most optimum way to run the machine combining hydraulic and mechanical performances.

It is also very common in several countries such as Brazil and China to have the machine operating conditions being defined by a dispatcher agency. For that cases it is particularly important to conduct the prototype diagnosis and influence the operating definitions from a structural mechanics and maintenance point of view.

It is also important to mention that during the diagnosis the air injection or natural air admission can be measured and tested. Air admission can smooth the unstable operating points and this evaluation, although predicted during the model test, must be tailored during prototype test where cause and effect are adequately correlated.

The Technological Research Institute of the State of Sao Paulo (IPT), a 105 years old non-profit institution owned by the of the state government, performed innumerous hydro machine diagnosis in tight collaboration with energy companies and the hydro machinery industry. The diagnosis experience of IPT is supported by over 15 measured Francis runners and stay vanes conducted in units from 47 MW up to over 700 MW since 1978. Voith Siemens (VSH) is a joint venture full liner company of Voith (137 years old) and Siemens (157 years old) that designs, manufactures, installs and operates hydro units. VSH uses to work in collaboration with measurement specialists such as the Naval and Oceanic group of IPT and also performed measurements by itself on Francis machines of different sizes, always focusing on findings that increase the reliability of the hydro unit.

A method to acquire correct information and how to get and find out important conclusions from the collected data is presented. Also some recommendations based on conclusions taken from several machines investigated around the world are presented at the end.

## 2. Measurement Techniques

The instrumentation system consists of data acquisition units, which have their own IP addresses and communicate with a notebook using Internet protocol. The system allows simultaneous measurement of up to 256 channels with more than 1000 samples/second per sensor if all sensors are used. If the number of channels decreases it is possible to increase the sampling rate (90 channels with 4096 samples/second per sensor).

The measurement strategy involves strain gages that are submerged in water, pressure transducers, mini waterproof pressure transducers, accelerometers and approximation meters. It is very important to measure all quantities with adequate equipment that synchronizes all data and so that the physical information can be correctly calibrated to the acquired data. It is also clear that an entire hydro machine diagnosis requires that all these measurements must be acquired at the same time in order to allow correct correlation of measurement data with the physical data. "Figure 5" shows the typical location of the measurement sensors installed in the power unit.



Figure 5 - Location of Sensors on Francis unit

Waterproof rosettes and unidirectional strain-gages are used for measuring strain on the runner and torsion strain of the turbine shaft (torque). These kind of strain-gages are attached to the runner blades, submerged in water, and the wires that come out from each strain gage are connected to signal conditioners. Strain gages and cables are totally covered with a special resin that provides mechanical and electrical isolation.

Since Francis runners are subject to high loads it is necessary to search the correct position of each strain-gage to be attached to runner blades. Typically the stress distribution of a Francis runner has a high gradient shape and it is necessary to know the mechanical structure in order to select the correct location for each strain gage. A remark must be made : every runner has a different stress field and this is related to the blade geometry and its particularities. With the evolution of computational fluid dynamics in the last decades several new geometries were developed mainly focusing higher efficiencies inclusively at part loads. This means that the prototype measurement campaign must be tailored according to the power unit conditions and especially according to the runner. The stress analysis must also be conducted in several loading conditions in order to search adequately the highest stressed points and attach on that location the strain gage. Modal analysis data must also be used in order to specify the most interesting position for the strain gage. The current calculation methods are accurate enough to predict within mm the stress location and this accuracy is highly dependent of the calculated flow and pressure distribution that is computed on CFD systems. This information needs to be cross checked with metallurgical data especially at the welded seams. Once the stress field is know the welding seam regions such as the transition area and the thermal affected zone (TAZ) must be identified in order to precisely guide the introduction of the strain gages.



Figure 6 - Strain Gages guided by structural analysis



Figure 7 - Resin Putty protection



Figure 8 – Strain Gages for runner entrance edge

Figure 9 – Strain gages for mode shape investigation

Pressure transducers are used to measure pressure (spiral case, head cover, draft tube, crown) and accelerometers to measure acceleration and vibration (band, crown, bearings). Mini pressure transducers can be also used for local under water dynamic acquisition. Power, speed and wicket gate opening (governor) are also simultaneously measured. All pressure transducers and proximeters must be calibrated before starting measurement. Their static outputs need to be also correlated with the current head level or distances for instance in order to guarantee that the quantities can be compared to reference values adequately.

In many examples the machine diagnosis as described here is combined with the relative efficiency test generally called "index test". Here the flow is also measured by the acquisition of pressure in two different locations of the inlet pipe of the spiral case by the use of a Winter Kenedy sensor. This differential pressure that is being measured can be correlated with measured flow obtained during the model test in the laboratory and discharge is obtained. The machine diagnosis is then suitable for the determination of relative efficiency values. Natural airflow, typically through the shaft can be also measured by an anemometer directly of at least by the acquisition of air gap opening of the aerating valve. This data will provide additional important information for the machine stability investigation.

The signal conditioners (for the strain-gages, accelerometers and pressure transducers on blades) are plugged inside control units installed on top of the generator shaft and rotate together with the runner, acquiring data, "fig. 10".

Other control units, not rotating with the runner, are used for measuring power, speed, opening, pressure, shaft oscillation, strain on stay vanes and any other sensor placed outside the turbine, "fig 11".

One of the control units called "master" sends a synchronization signal via cable to other control units on top of the shaft and, via "slip-ring", to the external control unit, so that all signals are simultaneously sampled, in every measurement. The measured signals outputted by each control unit are sent to a "hub" and from it to the "PC Card" of a notebook, where all signals are stored and real time displayed both in time and frequency domain.





Figure 10 - Measurement Control unit at the generator top

Figure 11 - Non rotating sensors conditioners

Each sensor from the runner is connected to an individual signal conditioner (each strain-gage is connected via shielded twisted conductors, using the three-wire method), where the signals are automatically balanced, amplified, calibrated and low-pass filtered (anti-aliasing). The cut-off frequency depends on the signal bandwidth of interest, which is tailored for each measured machine according to the design conditions.

From the conditioners the signals are sent to an analog to digital converter, where they are simultaneously sampled (1024 to 4096 samples per second, per sensor), multiplexed, converted to digital serial form (with 16 bits resolution), then formatted and finally sent, via slip-ring to a "hub" and then to a notebook, to be displayed and stored in data files. Signals from the sensors outside the turbine are filtered, sampled and converted simultaneously with the sensors on the runner and sent to the notebook via cable through the same "hub".

During measurements signals are real time displayed on the screen both in time and frequency domain, side by side. They may be organized in groups of channels to be displayed together and with a simple mouse click it is very easy to change the set of channels displayed on the screen.

Before starting measurement, the strain-gages are balanced and calibrated with the runner stopped and then recorded as the reference ("zero").

## 2.1. Measurement campaign method

Due to the fact that some strain gages, pressure transducers or even accelerometers will acquire data submerged in water and although every putty protection still has some limitations it is very important to plan adequately the measurement sequences so that all objectives are fulfilled in the first 2 measurement hours.

Typical prototype measurement goals are related to the determination of following quantities:

- Mean stress at runner blades and stay vanes at steady state operating conditions.
- Low frequency pressure pulsations at the draft tube and its effect on unit stability.
- Characteristic stress amplitudes of high stressed areas at runner blades and vanes.
- Dominant frequencies on rotating and non rotating parts with special focus on high frequency phenomena.
- Stresses and pressure pulsations developed during starting up and stopping transients.
- Dynamic stresses developed under speed no load conditions.
- Effect of different wicket gate opening periods on stresses and pressure pulsations for transients.
- Effects of air injection or natural air admission on every steady state for machine dynamics.
- Correlation of unit vibrations with possible causes such as pressure pulsations or other phenomena.

Steady state conditions and transient conditions need to be investigated. For the measurements the governor must be put in constant opening mode because it is necessary to make sure that the wicket gates operate in fixed position and this will keep same hydraulic flow conditions. The first part of the test consists to start the machine up to nominal rotation without synchronization, maintain this condition for few minutes and stop the machine. After this first step all sensors must be reviewed and the acquired data must be analyzed. The second step is to start the machine, synchronize it and increase power up to maximum power, maintain for few minutes and decrease the power step by step. The steps at this time must be selected based on the machine hydraulics. The machine opening should be kept constant at each step for 3 minutes in order to allow adequate FFT computation for frequency domain analysis.

After this second phase the entire strain scenario is evaluated and a dominant frequency analysis might be performed at the most important steady states. Now, deep investigation can be performed by selecting certain operating regions maintain the machine at these specific points for some minutes. At the end a load rejection of full load is recommended for investigation. At the end of the measurements, with the runner stopped, the reference signal must be recorded again.

Results are presented as time series graphs, tables and graphs of frequency spectra, waterfall graphs, average, characteristic amplitude, rms, standard deviation, maximum and minimum values. Results from strain-gages may also be expressed in stress. For example, principal stress and equivalent stress versus time (dynamic) can be computed using the instantaneous data measured. Frequency spectra and graphs of the stresses may then be obtained.

## 3. Typical machine stability analysis

Due to the fact that the method allows one to observe all sensors during machine operation in real time some conclusions can be taken right after the test. High and low exciting frequencies can be verified during the test and the relative efficiency results could also be forecast with good accuracy during the test using the mean observed values of the differential pressure transducer. However one important observation is the adequate set up of the sampling rate and the filter cutoff frequency. For that purpose the following excitation frequencies should be considered: Wicket gate passing frequency up to the 3<sup>rd</sup> harmonics, electrical frequency, vortex rope frequency (Rheinghans), machine runaway, over speed frequency and the possible von Karman excitation frequencies.

The observation limits will be set up by the filter cutoff frequency and if the occurrence of high frequency phenomena is going to be investigated the von Karman frequencies defined by (1) must be considered for the cutoff frequency set up. The von Karman frequency is calculated by (1) from the Strouhal number, the local flow velocity in m/s and the runner blade outlet thickness. Typically the computation of the possible von Karman excitation frequencies must be done for every load condition and for several areas along the blade discharge edge. These frequencies need then to be compared with the runner natural frequencies in water in order to evaluate the chances to have a natural mode shape being excited by any von Karman frequency.

$$f = S_r \frac{V}{d} \tag{1}$$

where Sr = 0.2 - 0.24.

"Figure 12" shows result example of a Francis machine. These time series are related to a machine start and stop excursion inclusively with a full load rejection and came from static pressure transducers, positioning sensors and strain gages. The first curve from top to bottom shows the power variation, the second the speed variation and the third one the wicket gate opening values acquired with a special positioning sensor. These three curves are the reference data for the investigation of pressure and strain variation along the entire test excursion. The last three curves show respectively the pressure variation at the draft tube near to the inspection door, the strains measured at one blade near to its welding seam at the crown and the strains measured on a stay vane at the pressure trailing edge side. The excursion permits to get the total variation of the measured quantities and shortly understand the machine behavior along the power ramp. For instance, the pressure draft tube curve has on this time series high amplitudes up to 200 MW of power, and has lower amplitudes when power increases to maximum getting again very intense dynamic portions during and after load rejection when the machine is hydraulically back to same condition as the starting one. This behavior typically transmits the vortex rope behavior in the draft tube showing considerable pressure fluctuations during low loads. An instantaneous peak can be observed during load rejection, an instantaneous rapid effect of shock waves generated at rapid transients.



Figure 12 – Power Ramp on a Francis Machine

The strain curve of the blade shows compression higher than 100 MPa during the initial operating phase, called "speed no load" (SNL) and a variation in tension direction as the power increases. At maximum power this strain gage shows approximately 100 MPa of tension stress. During the load rejection the blade experiments a transient stress fluctuation that is over 200 MPa coming back to the compression state and slowing down to zero when the machine stop as it would be expected. This curve shows two main subjects. There is a high frequency dynamic strain amplitude variation that is also larger during the same period when the pressure in the draft tube gets rough, smoothing out as soon the machine gets to maximum power. And there is a low frequency amplitude variation from start to stop that made the blade experienced a total compression to tension excursion. A fatigue calculation based on that curve can show if the low frequency variation is more dangerous to the runner blade material or if the high frequency variation is the one that causes more damage. On this particular case machine start and stop cycles are more critical to the blade material since the high frequency amplitudes are small and even this frequency value is not critical too.

The last curve shows the strain variation at the stay vanes where little higher dynamic amplitudes were observed during the period when the machine stayed at maximum power. Here an influence of higher velocities on larger openings increased the vibration at the stay vanes. Differently from the blades no compression-tension low frequency cycle was observed. However frequency analysis must also be conducted in order to investigate the fatigue accumulated damages to the material.

Machine stability can also be cross checked with the observations of "fig. 12" when the data of the accelerometers and approximation sensors that are connected to the guide bearings are plotted. Low frequency pressure pulsations contain a higher amount of energy sufficient to influence the overall machine behavior. The high frequency phenomena are more often related to local problems and local material damages while the low frequency phenomena are felt on the entire machine. "Figure 13" shows the shaft relative and absolute vibration in radial and axial direction measured at the turbine and generator guide bearing of the same example used at "fig. 12". The first curve is the reference power variation, the second and the third ones are the shaft relative bearing displacements in radial direction at 0 and 90 degrees. The fourth curve shows the axial vibration of the unit and the fifth the radial vibration still measured at the turbine bearing. The two last curves show the shaft displacements at the generator bearing gap, which probably increases its oil temperature. On this particular example, with power increase up to 250 MW the machine gets smoother, however relative shaft displacements get higher again near to 300-350 MW but the absolute vibration continues getting smaller. Here the shaft orbit goes to a precession shape. Above that region the machine gets again very stable even considering the shaft displacements. At the load rejection transient high vibrations and displacements are noticed getting to the SNL condition. After unit shut down, in this particular example, no amplitude was recorded.

At other examples (Fisher *et al.*, 2002), the machine passed a high vibration situation during the stopping sequence due to resonance with high frequency phenomena. Due to the existence of such possibility all machine transients must be studied carefully. "Figure 14" shows the runner strains results of three blades at the pressure and suction side near to the crown connection. All three consecutive curves show the same aspect, fact that is common for machined blades due to the achievement of tight manufacturing tolerances. Also the blades are under the same effect on the pressure and suction sides with higher amplitudes being experienced at the suction blade side. The trend of the stresses is in accordance with the finite element calculation.



Figure 13 -Shaft vibration during power excursion Figure 14 -Strains at 3 consecutive blades = Same behavior

There are some excitation frequencies that are going to be present during the machine operation. The goal of the diagnosis is to check if these excitations are going to be amplified by resonance. The wicket gate passing frequency and harmonics are going to excite the rotating parts. "Figure 15" demonstrates a typical waterfall diagram in the frequency domain where it is possible to recognize the wicket gate exciting frequency growing up as the flow velocity and power increases.

A dynamic stress variation of 3% up to 8% of the mean stress portion while the machine is running at the rated operating point is considered within acceptable material limits. Higher values of these amplitudes would indicate amplification and possible damages to the runner material. During part load or low load the stress amplitudes up to the wicket gate passing frequency (rotation x number of wicket gates) should not be higher than 20% of the mean stress. The machine operating time at this region is limited exactly due to the presence of such instability. Long term operation at this condition will probably cause damages to the material structure of the runner, even for a high strength material such as the ASTM A743 CA6NM series that have yield point above 550 MPa and high toughness typically over 100 J.



Figure 15 - Water Fall – Discharge edge band

Figure 16 – Water Fall – Discharge Edge Crown

High frequency phenomena such as the presence of von Karman trailing edge vortex are commonly over 200Hz and might get higher according to machine size and rotation speed. This high frequency excitation, if containing sufficient energy to excite the blades or even to excite a blade natural frequency, can seriously damage the runner causing cracks at the most stressed areas after some months of operation. The occurrence of such phenomena is totally dependent of the runner design and it needs to be avoided in order to enable adequate runner lifetime.

"Figure 17" shows two time series that are related to strain-gage responses that were connected to runner high stress areas. The upper series shows a mean stress of ca. 100 MPa that occurs at 160 MW and the second curve below shows the mean stress values near to 70MPa occurring at 150 MW. These mean values are within the material acceptable limits , however this figure does not permit one to check the frequency and apparently the upper curve represents the critical one for the component lifetime. By checking "fig 18", one will see that for the same machine the stresses measured at the same blade location for 130MW and for 150MW contain high frequency fluctuation of 200 Hz with peak to peak amplitude over 40%. The upper curve although showing higher mean stresses does not contain a periodic fluctuation and the stress amplitude is at 5%, which is acceptable for the runner material. "Figure 19" shows the frequency domain results of several time series from 0 up to 160 MW. This figure clearly shows that the high frequency excitation starts to occur at 110 MW and stops at 160MW. The amplitudes increase from 110 MW up to 150 MW stopping suddenly at 160 MW and this is a phenomena that is dependent from the local flow velocity.



Figure 17 – High and lower mean stresses

Figure 18 – High frequency amplitude for lower mean stresses

A typical water fall diagram obtained from strain gages that do not feel any high frequency excitation is given on "fig. 20". This diagram shows the dynamics recorded at runner entrance edges where, in the absence of hydraulic problems, this kind of effect is not percepted inclusively concerning the effects of the rope.



Figure 19 - Water fall-high frequency phenomena

Figure 20 - Water fall-Aspect without high frequency

These interpretation examples summarize briefly the machine most important diagnosis focus. These data when used for fatigue calculations can predict with reasonable accuracy the lifetime of the runner blade and the coupled maintenance cost to repair the damaged areas. Other goals such as the investigation of low and high frequency phenomena on specific operating regions are also commonly added to the diagnosis goals, together with the analysis of machine stability and stress reactions when air is injected through the bottom ring, turbine head cover or admitted though the shaft.

## 4. Conclusions & Recommendations

The acquisition method for a machine diagnosis was described highlighting the set ups and adjustments that must be conducted in order to allow adequate cause-effect correlations. An overview of how a measurement campaign must be planned and how it needs to be tailored for a specific Francis machine was demonstrated. Some interpretation examples were shared in order to demonstrate how the data can be used to better understand machine behavior and operational effects since all accumulated experience and knowledge in this specific field is still under high development.

The recommendation for the energy companies is to consider a full machine diagnosis, especially for Francis units, as it is being done frequently in new power plants in the far east, as part of a measure to assure full understanding of hydraulic and structure mechanical behavior and to tailor the unit operating mode by the use of this acquired knowledge in order to optimize the return of investment and keep the maintenance under comfortable limits.

## 5. References

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#### 6. Responsibility notice

The first author is the only responsible for the data included in this paper. All presented data are accumulated from several experiences and do not correspond to any specific machine. The only aim of this paper is to illustrate the method and corresponding interpretation.